

classmate

Date _____

Page _____

DATA LOGICS AND MICRO- PROCESSORS

SharkCoders

Join our whatsapp group

Excess 3 - codes

Q. Convert (15)₁₀ in excess-3 code.

1	5
+ 3	+ 3
4	8
↓	↓
0100	1000

∴ (15)₁₀ = (01001000)₂

Q. Convert (231.75)₁₀ to excess-3 code.

2	3	1	.	7	5
+ 3	+ 3	+ 3		+ 3	+ 3
5	6	4	.	10	8
↓	↓	↓	↓	↓	↓
0101	0110	0100	.	1010	1000

∴ (231.75)₁₀ = (010101100100.10101000)

Q. Reverse: 110010100011.01110101

1	1	0	0	1	0	1	0	0	0	1	1	.	0	1	1	1	0	1	0	1
↓	↓	↓	↓	↓	↓	↓	↓	↓	↓	↓	↓	↓	↓	↓	↓	↓	↓	↓	↓	↓
12	10	3	3	7	5	4	2	0	0	0	0	0	0	0	0	0	0	0	0	0
- 3	- 3	- 3	- 3	- 3	- 3	- 3	- 3	- 3	- 3	- 3	- 3	- 3	- 3	- 3	- 3	- 3	- 3	- 3	- 3	- 3
9	7	0	0	4	2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

(110010100011.01110101)₂ = (970.42)₁₀

SUMMARY

- 3 excess codes & reverse
- gray code & reverse
- all gates
- by using NAND and NOR gates...
- SOP
- POS
- K-Map
- Half adder
- Full adder

SharkCoders

18/7/24

classmate

Date _____
Page _____

Turning to hexadecimal...

16	970	10
16	60	12
16	3	3
	0	

$$\rightarrow (3(12)(10))_{16} = (3CA)_{16}$$

$$.42 \rightarrow (.6B851E)$$

$$\begin{array}{r} .42 \\ \times 16 \\ \hline 6.72 \end{array}$$

$$\downarrow \times 16$$

$$(6) 11.52$$

$$\downarrow \times 16$$

$$(11) 8.32$$

$$\downarrow \times 16$$

$$(8) 5.12$$

$$\downarrow \times 16$$

$$(5) 1.92$$

$$\downarrow \times 16$$

$$(1) 14.72$$

$$\downarrow \times 16$$

$$(14) 11.52$$

$$.42$$

1

$$\therefore (970.42)_{10} = (3CA.6B851E)_{16}$$

Gray Codes

- this is to secure our data.

- these codes are implemented

- only one bit change in 2 successive numbers.

- reduce switching frequencies.

- Conversions

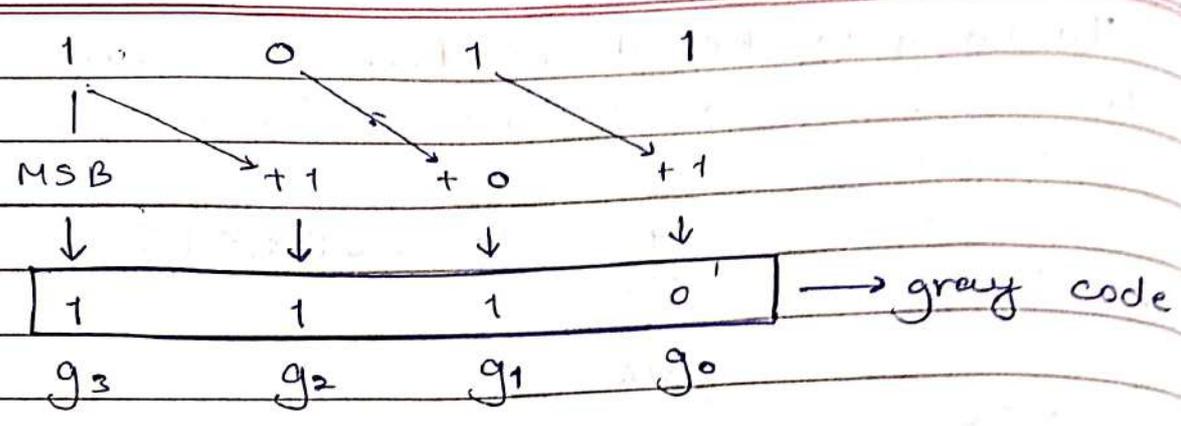
1: Take MSB as it is

2: Add MSB to the next bit

3: Write the sum and ignore the carry

4: Repeat.

Q. $(1011)_2 \rightarrow$ gray code.



$A \oplus B = A\bar{B} + \bar{A}B = Y$

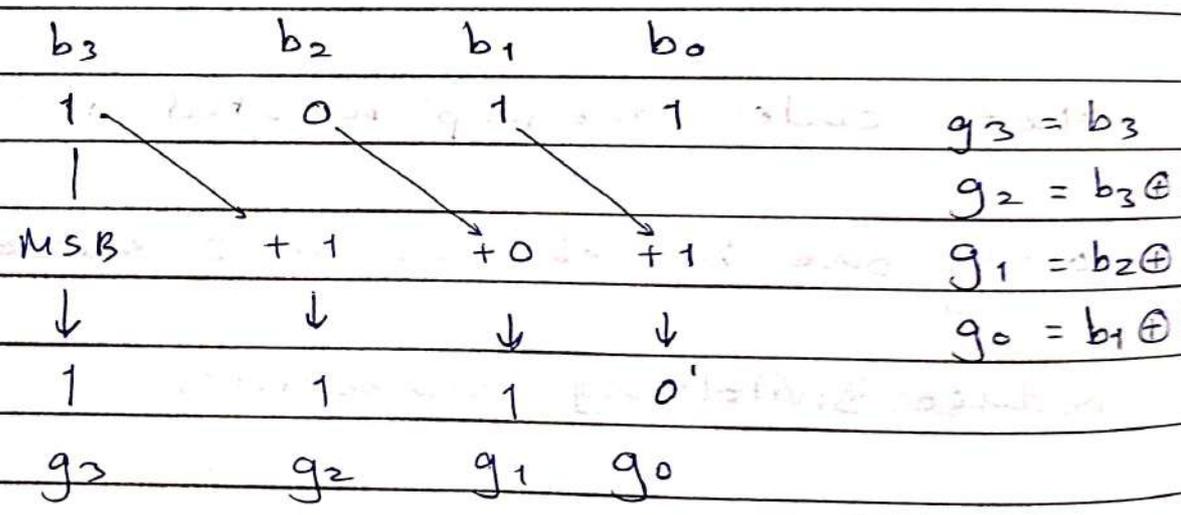
A	B	Y
0	0	0
0	1	1
1	0	1
1	1	0

when no of 1s odd $\Rightarrow 1$
 otherwise $\Rightarrow 0$

↓

a.k.a. odd 1's detector

SharkCoders

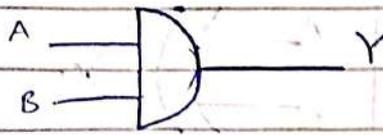


Logic Gates

Acts as a building block for digital circuits.

AND Gate

• symbol:

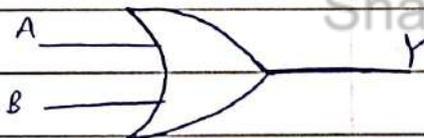


• truth table:

A	B	Y
0	0	0
0	1	0
1	0	0
1	1	1

OR Gate

• symbol:

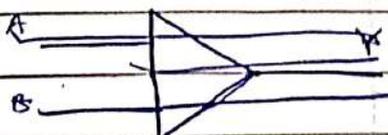


• truth table

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	1

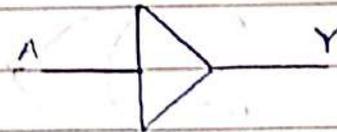
NOT Gate

• symbol:



NOT Gate

• symbol:

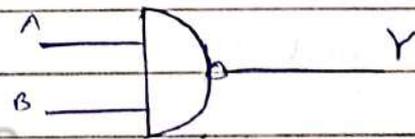


• truth table:

A	Y
0	1
1	0

NAND Gate

• symbol:



• truth table:

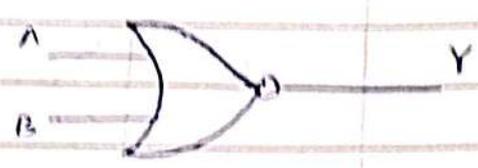
A	B	Y
0	0	1
0	1	1
1	0	1
1	1	0

• truth table:

A	B	Y
0	0	
0	1	
1	0	
1	1	

NOR Gate

• symbol:

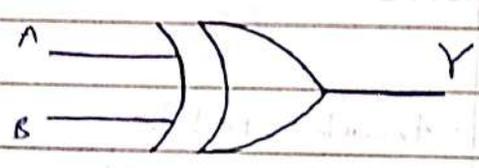


• truth table:

A	B	Y
0	0	1
0	1	0
1	0	0
1	1	0

XOR Gate

• symbol:

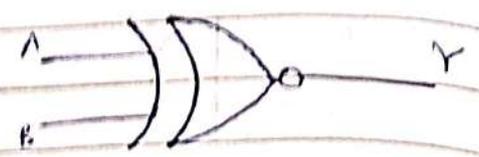


• truth table

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	0

X-NOR Gate

• symbol:



• truth table:

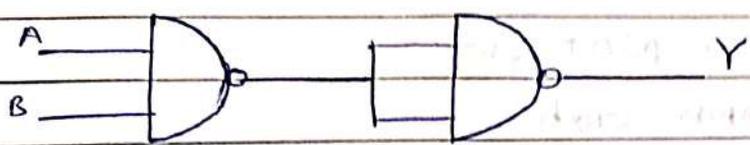
A	B	Y
0	0	1
0	1	0
1	0	0
1	1	1

Universal Gates

NAND and NOR gates are called universal as any digital circuit can be implemented by using these two gates.

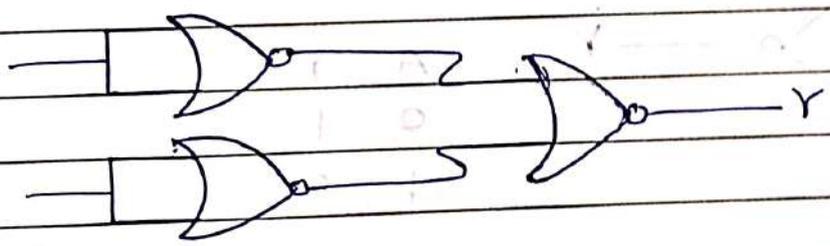
Implementation of AND Gates:

a) By using NAND Gates only



A	B	Y
0	0	0
0	1	0
1	0	0
1	1	1

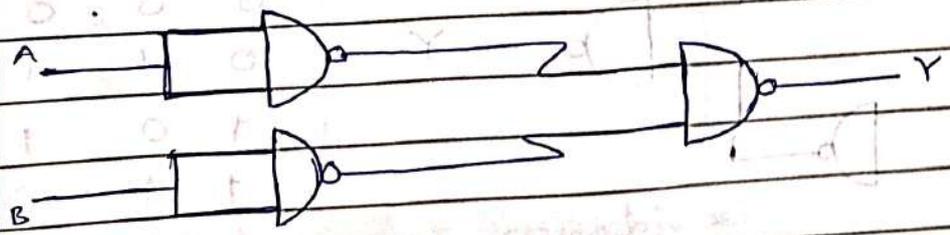
b) By using NOR Gates only



A	B	Y
0	0	0
0	1	0
1	0	0
1	1	1

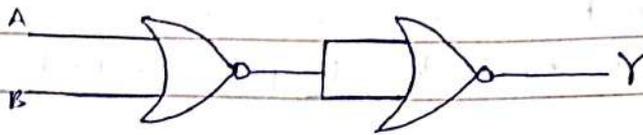
Implementation of OR Gate

a) By using NAND Gates only



A	B	Y
0	0	0
0	1	1
1	0	1
1	1	1

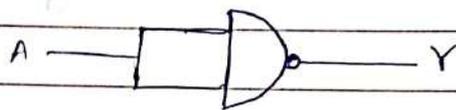
b) By using NOR Gates only



A	B	Y
0	0	0
0	1	1
1	0	1
1	1	1

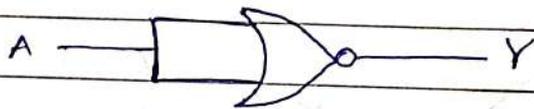
Implementation of NOT Gates:

a) By using NAND Gate



A	Y
0	1
1	0

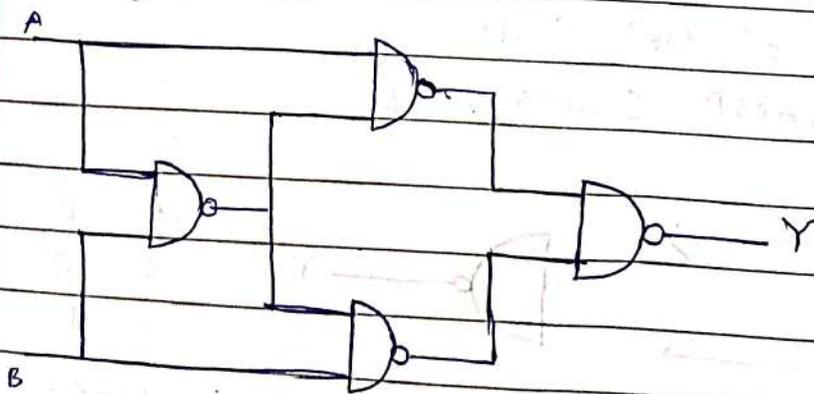
b) By using NOR Gate



A	Y
0	1
1	0

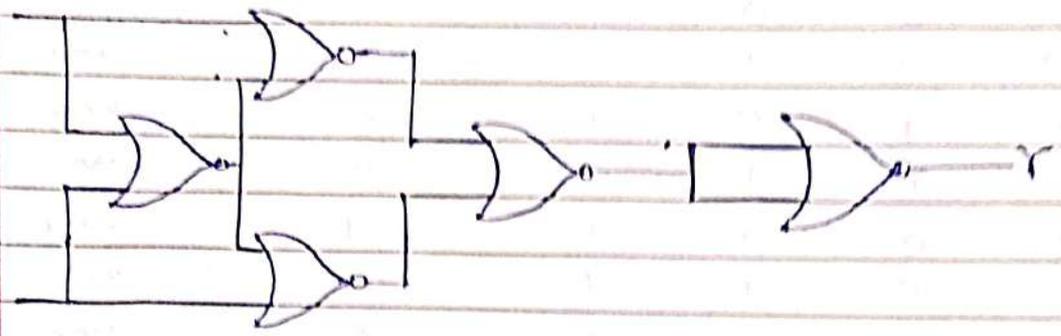
Implementation of XOR Gates:

a) By using NAND Gate



A	B	Y
0	0	0
0	1	1
1	0	1
1	1	0

b) By using NOR Gate

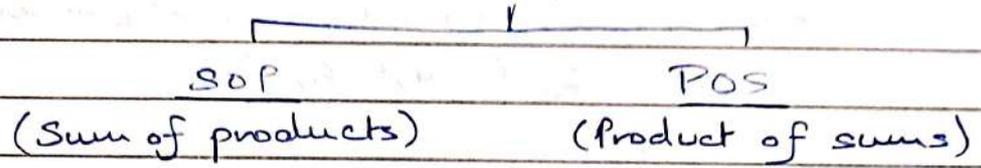


A	B	Y
0	0	0
0	1	1
1	0	1
1	1	0

29/7/24 Boolean funcⁿ and representation

SharkCoders

Boolean funcⁿ



Sum of products (SOP):

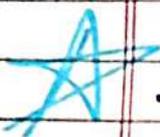
$$\bar{A} \cdot B \cdot \bar{C} + A \cdot \bar{B} \cdot C + A \cdot B \cdot C$$

A	S/P	O/P
B		Y
a		

• total no. of combination = 2^n where
 n = no. of variables

(Example) ↘

A	B	C	Y	Decimal	Min terms
0	0	0	0	0	m_0
0	0	1	0	1	m_1
0	1	0	1	2	m_2
0	1	1	0	3	m_3
1	0	0	1	4	m_4
1	0	1	1	5	m_5
1	1	0	1	6	m_6
1	1	1	1	7	m_7



• Standardized / Canonical form:

$$F(A, B, C) = \bar{A} \cdot \bar{B} \cdot \bar{C} + A \cdot \bar{B} \cdot \bar{C} + A \cdot \bar{B} \cdot C + \bar{A} \cdot B \cdot \bar{C} + A \cdot B \cdot C$$

- consider only the high values of Y
- write their expressions and add.

→ in min. form:-

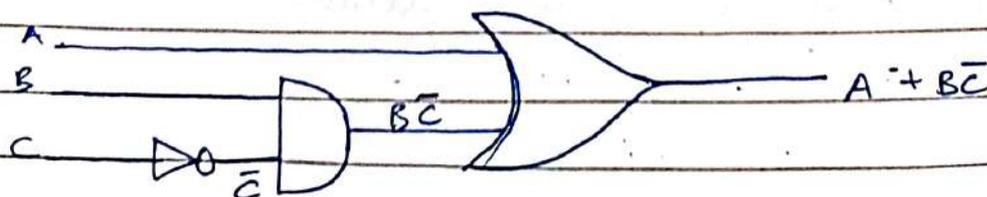
$$F(A, B, C) = m_2 + m_4 + m_5 + m_6 + m_7 = \sum_m (2, 4, 5, 6, 7)$$



• Non-canonical / minimal SOP form:

$$\begin{aligned} F(A, B, C) &= \bar{A} \cdot B \cdot \bar{C} + A \cdot \bar{B} \cdot \bar{C} + A \cdot \bar{B} \cdot C + A \cdot B \cdot \bar{C} + A \cdot B \cdot C \\ &= \bar{A} \cdot B \cdot \bar{C} + A \cdot \bar{B} (\bar{C} + C) + AB (\bar{C} + C) \\ &= \bar{A} \cdot B \cdot \bar{C} + A \cdot \bar{B} (1) + AB (1) \\ &= \bar{A} \cdot B \cdot \bar{C} + A (\bar{B} + B) \\ &= \bar{A} \cdot B \cdot \bar{C} + A \quad [\bar{A} (B \cdot \bar{C}) + A = A + B \cdot \bar{C}] \\ &= A + B \cdot \bar{C} \end{aligned}$$

- this is the reduced form of canonical form.
- representation



Q. Simplify the expression:

$$Y(A, B) = \sum_m (0, 2, 3)$$

Ans combinations = $2^2 = 4$

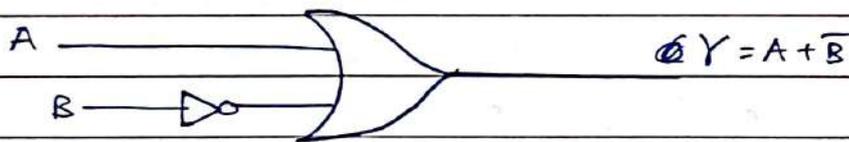
A	B	Y	min terms	Decimal
0	0	1	m_0	0
0	1	0	m_1	1
1	0	1	m_2	2
1	1	1	m_3	3

$$\begin{aligned} F(A, B) &= \bar{A} \cdot \bar{B} + A \cdot \bar{B} + A \cdot B \\ &= \bar{A} \cdot \bar{B} + A(\bar{B} + B) \\ &= \bar{A} \cdot \bar{B} + A(1) \\ &= A + \bar{B} \end{aligned}$$

$$[\bar{A}X + AX = A + X]$$

\therefore The simplified expression is $A + \bar{B}$.

Representation:

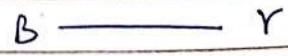


Q. For the given truth table, minimize the SOP operation.

A	A	B	Y	Decimal
	0	0	0	0
	0	1	1	1
	1	0	0	2
	1	1	1	3

Ans.
$$\begin{aligned} F(A, B) &= \sum_m (1, 3) \\ &= \bar{A} \cdot B + A \cdot B \\ &= B(\bar{A} + A) = B \end{aligned}$$

Representation:

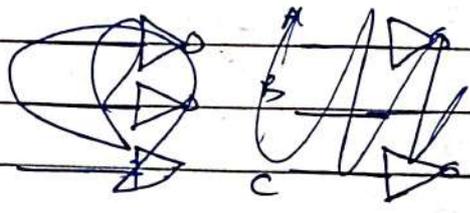


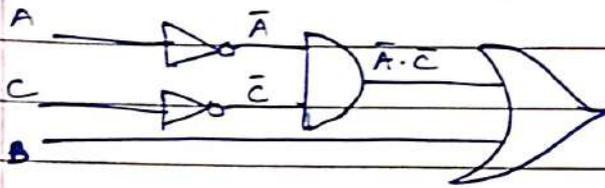
Q. $Y(A, B, C) = \sum_m (0, 2, 3, 6, 7)$

A	B	C	Y	min
0	0	0	1	m_0
0	0	1	0	m_1
0	1	0	1	m_2
0	1	1	1	m_3
1	0	0	0	m_4
1	0	1	0	m_5
1	1	0	1	m_6
1	1	1	1	m_7

$$\begin{aligned}
 F(A, B, C) &= \bar{A} \cdot \bar{B} \cdot \bar{C} + \bar{A} \cdot B \cdot \bar{C} + \bar{A} \cdot B \cdot C + A \cdot B \cdot \bar{C} + A \cdot B \cdot C \\
 &= \bar{A} \cdot \bar{B} \cdot \bar{C} + \bar{A} \cdot B (\bar{C} + C) + A \cdot B (\bar{C} + C) \\
 &= \bar{A} \cdot \bar{B} \cdot \bar{C} + \bar{A} \cdot B + A \cdot B \\
 &= \bar{A} \cdot \bar{B} \cdot \bar{C} + B \\
 &= B + \bar{A} \cdot \bar{C}
 \end{aligned}$$

Representation:





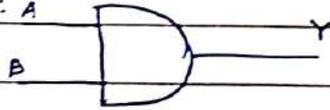
$$Y = B + \bar{A} \cdot \bar{C}$$

U74HC08L-01:

DLM Lab

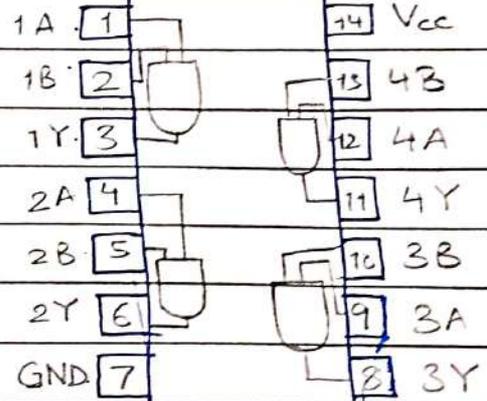
AND

Symbol: A



Truth table:

A	B	Y
0	0	0
0	1	0
1	0	0
1	1	1

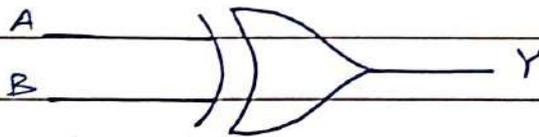


Funcⁿ table:

I/P (A)	I/P (B)	O/P
H	H	H
H	L	L
L	H	L
L	L	L

X-OR

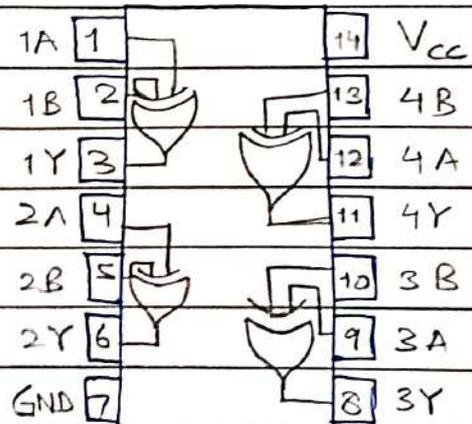
Symbol:



Truth table:

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	0

SN54HC86N:



2/8/24 .

classmate

Date _____

Page _____

Solving one problem with SOP and POS

A	B	C	Y	m	SOP
1	1	1	1	m_0	$A \cdot B \cdot C$
1	1	0	0	m_1	$\bar{A} \cdot B \cdot \bar{C}$
1	0	1	1	m_2	$A \cdot \bar{B} \cdot C$
1	0	0	1	m_3	$A \cdot \bar{B} \cdot \bar{C}$
0	1	1	0	m_4	$\bar{A} \cdot B \cdot C$
0	1	0	0	m_5	$\bar{A} \cdot B \cdot \bar{C}$
0	0	1	1	m_6	$\bar{A} \cdot \bar{B} \cdot C$
0	0	0	1	m_7	$\bar{A} \cdot \bar{B} \cdot \bar{C}$

$$Y(A, B, C) = \sum_m (0, 2, 3, 6, 7)$$

$$= (A \cdot B \cdot C) + (A \cdot \bar{B} \cdot C) + (A \cdot \bar{B} \cdot \bar{C}) + (\bar{A} \cdot \bar{B} \cdot C) + (\bar{A} \cdot \bar{B} \cdot \bar{C})$$

$$= AC(B + \bar{B}) + \bar{B} \cdot \bar{C}(A + \bar{A}) + \bar{A} \cdot \bar{B} \cdot C$$

$$= AC + \bar{B} \cdot \bar{C} + \bar{A} \cdot \bar{B} \cdot C$$

$$= \bar{B} \cdot \bar{C} + A \cdot C + \bar{B} \cdot C$$

$$= A \cdot C + \bar{B} \cdot C$$

$$= A \cdot C + \bar{B} \cdot (\bar{C} + C)$$

$$= A \cdot C + \bar{B} \cdot (C + \bar{A})$$

$$= A \cdot C + \bar{B} \cdot C + \bar{B} \cdot \bar{A}$$

=

Sharkcoders

A	B	C	Y	m	SOP
0	0	0	1	m ₀	A = 1 Ā = 0
0	0	1	0	m ₁	
0	1	0	1	m ₂	POS A = 0 Ā = 1
0	1	1	1	m ₃	
1	0	0	0	m ₄	
1	0	1	0	m ₅	
1	1	0	1	m ₆	
1	1	1	1	m ₇	

$$Y = \sum_m (0, 2, 3, 6, 7)$$

$$= m_0 + m_2 + m_3 + m_6 + m_7$$

$$= (\bar{A} \cdot \bar{B} \cdot \bar{C}) + (\bar{A} \cdot B \cdot \bar{C}) + (\bar{A} \cdot B \cdot C) + (A \cdot B \cdot \bar{C}) + (A \cdot B \cdot C)$$

$$= \bar{A} \cdot \bar{C} (B + B) + A \cdot B (\bar{C} + C) + (\bar{A} \cdot B \cdot C)$$

$$= \bar{A} \cdot \bar{C} + A \cdot B + \bar{A} \cdot B \cdot C$$

$$= B(A + \bar{A} \cdot C) + \bar{A} \cdot \bar{C}$$

$$= B(A + C) + \bar{A} \cdot \bar{C}$$

$$= B \cdot A + B \cdot C + \bar{A} \cdot \bar{C}$$

POS

$$Y = \prod M(1, 4, 5)$$

$$= (A + \bar{B} + \bar{C}) \cdot (\bar{A} + B + C) \cdot (\bar{A} \cdot \bar{B} \cdot \bar{C})$$

$$= (A + \bar{B} + \bar{C}) \cdot (\bar{A} + B) \cdot (C \bar{C})$$

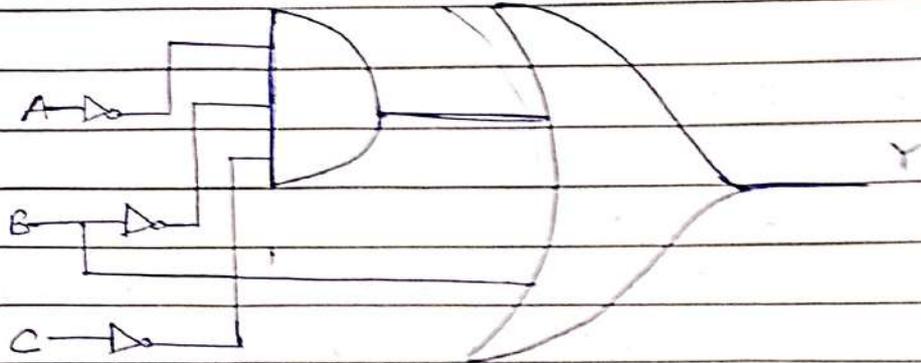
$$= (A + \bar{B} + \bar{C}) \cdot (\bar{A} + B) \cdot 0$$

$$= \bar{B} + (A \bar{C} \cdot \bar{A}) \cdot \bar{B} + (A + \bar{C}) \cdot \bar{A}$$

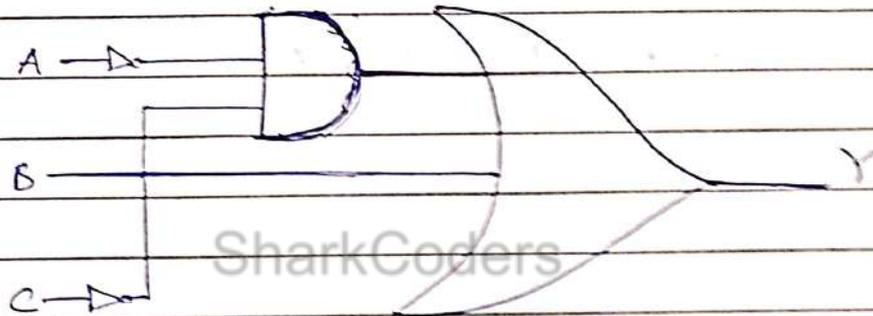
$$= \bar{B} + (0) + (\bar{A} \cdot \bar{C})$$

$$= \bar{B} + \bar{A} \bar{C}$$

SOP - $Y = \bar{A}\bar{B}\bar{C} + B$



POS - $\bar{A}\bar{C} + B$



P.	A	B	C	Y	m
	0	0	0	0	m_0
	0	0	1	1	m_1
	0	1	0	1	m_2
	0	1	1	1	m_3
	1	0	0	0	m_4
	1	0	1	1	m_5
	1	1	0	0	m_6
	1	1	1	1	m_7

$$\begin{aligned}
 Y(A, B, C) &= \sum_{m=0, 2, 3, 5, 7} \\
 &= (\bar{A} \cdot \bar{B} \cdot \bar{C}) + (\bar{A} \cdot B \cdot \bar{C}) + (\bar{A} \cdot B \cdot C) + (A \cdot \bar{B} \cdot \bar{C}) + (A \cdot B \cdot C) \\
 &= \bar{A} \cdot \bar{C} (\bar{B} + B) + A \cdot B (\bar{C} + C) + (\bar{A} \cdot \bar{B} \cdot \bar{C}) \\
 &= \bar{A} \cdot \bar{C} + A \cdot B + \bar{A} \cdot \bar{B} \cdot \bar{C}
 \end{aligned}$$

$$\overline{B + \overline{A \cdot B \cdot C}}$$

POS

$$A = 0 \quad \text{TFM}()$$

$$\overline{A} = 1$$

$$Y = \sum_m (1, 2, 3, 5, 7)$$

$$= (\overline{A} \cdot \overline{B} \cdot C) + (\overline{A} \cdot B \cdot \overline{C}) + (\overline{A} \cdot B \cdot C) + (A \cdot \overline{B} \cdot C) + (A \cdot B \cdot C)$$

$$= \overline{A} \cdot B (\overline{C} + C) + A \cdot C (\overline{B} + B) + (\overline{A} \cdot \overline{B} \cdot C)$$

$$= \overline{A} \cdot B + A \cdot C + (\overline{A} \cdot \overline{B} \cdot C)$$

$$= \overline{A} \cdot C (\overline{B} + B) + A \cdot C (\overline{B} + B) + (\overline{A} \cdot \overline{B} \cdot C)$$

$$= \overline{A} \cdot C + A \cdot C + \overline{A} \cdot \overline{B} \cdot C$$

$$= C + \overline{A} \cdot \overline{B} + \overline{A} \cdot \overline{B} \cdot C = C + \overline{A} \cdot \overline{B}$$

POS

$$A = 0$$

$$A = 1$$

SharkCoders

$$Y = \text{TFM}(0, 4, 6)$$

$$= M_0 + M_4 + M_6$$

$$= (A+B+C) \cdot (\overline{A} + \overline{B} + C)$$

$$= (A+B+C) \cdot (\overline{A} + \overline{B} + C)$$

$$= (B+C) + (A\overline{A}) \cdot (\overline{A} + \overline{B} + C)$$

$$= (B+C) \cdot (\overline{A} + \overline{B} + C)$$

$$= (C) \cdot (B) + (\overline{A} + \overline{B})$$

$$= C + (B\overline{A}) + (B\overline{B})$$

$$= \overline{A}B + C$$

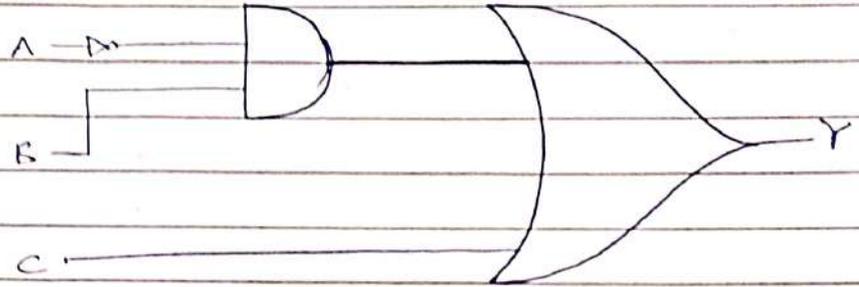
2/8/24

classmate

Date _____

Page _____

$$Y = C + \bar{A}B$$



$$Y = \bar{A}B$$

5/8/24 K-Map (Karnaugh Map)

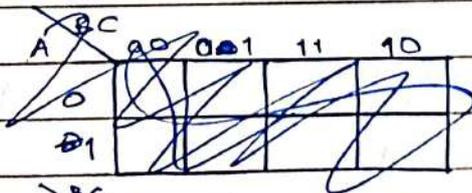
Pictorial representation method that is used to minimize various boolean expressions without using the boolean algebra theorems along with the eqⁿ manipulations.

- can be a special version of the truth table
- can easily minimize various expressions that have two or four variables.

E.g.: $F(A,B,C) = Y$

Works on gray codes

(only one digit changes)



	BC			
A	00	01	11	10
0	0	1	3	2
1	4	5	7	6

2² 2¹ 2⁰
4 2 1

→ m terms

A	B	C	Y	m
0	0	0	0	m ₀
0	0	1	0	m ₁
0	1	0	1	m ₂
0	1	1	0	m ₃
1	0	0	1	m ₄
1	0	1	1	m ₅
1	1	0	1	m ₆
1	1	1	0	m ₇

SOP:-

[A-1; A-0]

$$\begin{aligned}
 F(A, B, C) &= \sum_m = (2, 4, 5, 6) \\
 &= (\bar{A} \cdot \bar{B} \cdot \bar{C}) + (\bar{A} \cdot \bar{B} \cdot C) + (\bar{A} \cdot B \cdot \bar{C}) + (A \cdot B \cdot \bar{C}) \\
 &= \bar{A} \cdot \bar{C} (\bar{B} + B) + (\bar{A} \cdot B \cdot \bar{C}) + (A \cdot B \cdot \bar{C}) \\
 &= \bar{A} \cdot \bar{C} (\bar{A} + A) + (\bar{A} \cdot B \cdot \bar{C}) + (A \cdot B \cdot \bar{C}) \\
 &= \bar{A} \cdot \bar{C} + (\bar{A} \cdot B) (\bar{C} + C) \\
 &= \bar{A} \cdot \bar{C} + \bar{A} \cdot B
 \end{aligned}$$

POS:-

[A-1; A-0]

$$\begin{aligned}
 F(A, B, C) &= \prod M(0, 1, 3, 7) \\
 &= (\bar{A} \cdot \bar{B} \cdot \bar{C}) + (\bar{A} \cdot \bar{B} \cdot C) + (\bar{A} \cdot B \cdot C) + (A \cdot B \cdot C) \\
 &= (\bar{A} \cdot \bar{B}) (\bar{C} + C) + BC (\bar{A} + A) \\
 &= \bar{A} \cdot \bar{B} + BC \\
 &= (\bar{A} + \bar{B} + \bar{C}) \cdot (\bar{A} + \bar{B} + C) \cdot (\bar{A} + B + C) \cdot (A + B + C) \\
 &= \bar{A} + \bar{B} + (\bar{C} \cdot C) + B + C + (\bar{A} \cdot A) \\
 &= (\bar{A} + \bar{B}) + 0 + (B + C) + 0 \\
 &= \bar{A} + \bar{B} + B + C \quad (\bar{A} + \bar{B}) \cdot (B + C) \\
 &= \bar{A} + \bar{B} \cdot \bar{A} \cdot B + \bar{A} \cdot C + \bar{B} \cdot B + \bar{B} \cdot C \\
 &= \bar{A} \cdot B + \bar{A} \cdot C + \bar{B} \cdot C \\
 &= \bar{A} \cdot B + \bar{A} \cdot C + \bar{B} \cdot C
 \end{aligned}$$

5/2/24

classmate

Date _____

Page _____

K-Map

		BC				
	A	00	01	11	10	
0		0	0	0	1	B \bar{C}
1		1	1	0	1	
		A \bar{B}				

$$\therefore F(A, B, C) = Y = A\bar{B} + B\bar{C}$$

POS:-[$\bar{A}-1$; A-0]

A	B	C	Y	m
0	0	0	0	m ₀
0	0	1	0	m ₁
0	1	0	1	m ₂
0	1	1	0	m ₃
1	0	0	1	m ₄
1	0	1	1	m ₅
1	1	0	1	m ₆
1	1	1	0	m ₇

POS:-

$$F(A, B, C) = Y = \Pi M(0, 1, 3, 7)$$

$$= (A+B+C) \cdot (A+B+\bar{C}) \cdot (A+\bar{B}+\bar{C}) \cdot (\bar{A}+\bar{B}+\bar{C})$$

$$= [(A+B) + (C \cdot \bar{C})] \cdot [(\bar{B}+\bar{C}) + (A \cdot \bar{A})]$$

$$= (A+B) + (\bar{B}+\bar{C})$$

$$= A\bar{B} + A\bar{C} + B\bar{B} + B\bar{C}$$

$$= A\bar{B} + A\bar{C} + B\bar{C}$$

Q.	A	B	C	Y	m
	0	0	0	1	m ₀
	0	0	1	0	m ₁
	0	1	0	1	m ₂
	0	1	1	1	m ₃
	1	0	0	0	m ₄
	1	0	1	0	m ₅
	1	1	0	1	m ₆
	1	1	1	1	m ₇

K-Map :-

		BC			
A		00	01	11	10
0		000 1	001 0	011 1	010 1
1		100 0	101 0	111 1	110 1

$$\bar{A}\bar{C} + BC + B\bar{C} = F(A,B,C) = Y$$

8/8/24

A	B	C	Y	m
0	0	0	0	m ₀
0	0	1	1	m ₁
0	1	0	0	m ₂
0	1	1	1	m ₃
1	0	0	1	m ₄
1	0	1	1	m ₅
1	1	0	1	m ₆
1	1	1	0	m ₇

K-Map - (NEXT PAGE)

8/9/24

	BC	00	01	11	10
A		00	01	11	10
0		0	1	1	0
1		1	1	0	1

$F(A, B, C) = Y = A\bar{B} + \bar{A}C + A.B\bar{C}$

Q.

A	B	C	D	Y	m
0	0	0	0	0	m ₀
0	0	0	1	0	m ₁
0	0	1	0	0	m ₂
0	0	1	1	1	m ₃
0	1	0	0	0	m ₄
0	1	0	1	0	m ₅
0	1	1	0	1	m ₆
0	1	1	1	1	m ₇
1	0	0	0	1	m ₈
1	0	0	1	1	m ₉
1	0	1	0	0	m ₁₀
1	0	1	1	0	m ₁₁
1	1	0	0	0	m ₁₂
1	1	0	1	0	m ₁₃
1	1	1	0	1	m ₁₄
1	1	1	1	0	m ₁₅

	CD	00	01	11	10
AB					
00			1		
01			1	1	
11				1	
10		1	1		

SharkCoders

12/8/24 Half Adder

A combinational arithmetic circuit that adds two numbers and produces a sum width and a carry width. both at its output.

A	B	Sum	Carry
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1

Sum K-Map:-

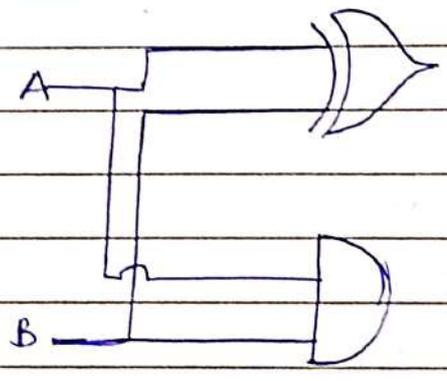
	B	0	1
A	0	0	1
1	1	1	0

$\bar{A}B + A\bar{B} = A \oplus B$

Carry K-Map:-

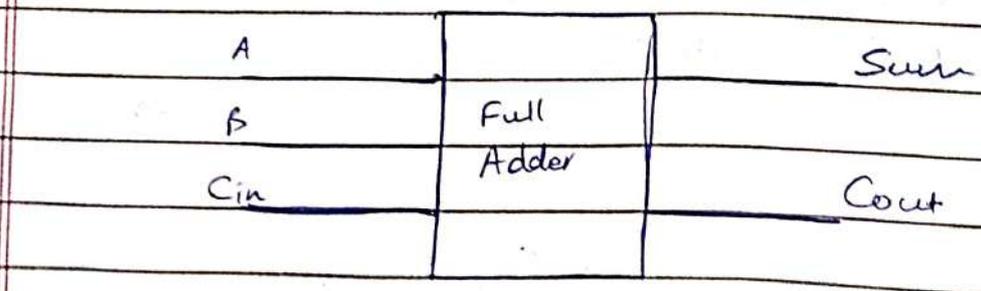
	B	0	1
A	0	0	0
1	0	0	1

$AB = A \wedge B$



Full Adder

A type of adder that adds 3 inputs and produces two outputs.



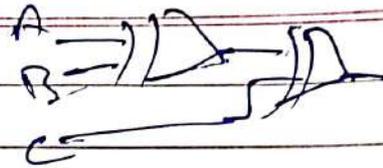
12/2/24

classmate

Date _____

Page _____

A	B	Cin	Sum	Cout	
0	0	0	0	0	0
0	0	1	1	0	1
0	1	0	1	0	2
0	1	1	0	1	3
1	0	0	1	0	4
1	0	1	0	1	5
1	1	0	0	1	6
1	1	1	1	1	7



Sum K-Map :-

		BCin			
		00	01	10	11
A	0	000	001	010	011
	1	100	101	110	111

$\bar{A} + A = A$

SharkCoders

Carry K-Map :-

		BCin			
		00	01	10	11
A	0	000	001	010	011
	1	100	101	110	111

$\bar{A}BCin + A$

$XOR = \bar{A}B + \bar{B}A = A \oplus B$

$XNOR = \bar{A}\bar{B} + AB = \overline{A \oplus B}$

Sum K-Map :-

		BCin			
		00	01	11	10
A	0	000	001	011	010
	1	100	101	111	110

$ABCin + \bar{A}\bar{B}Cin + A\bar{B}Cin + \bar{A}B\bar{C}in$

$\bar{B}Cin$

$A\bar{C}in(\bar{B} + B) + \bar{A}Cin(\bar{B} + B)$

$= Cin(\bar{A}\bar{B} + \bar{A}B) + Cin(AB + \bar{A}\bar{B})$

$= Cin \times XOR(A \times XOR B)$

$= A \oplus B \oplus Cin$

$= Cin(A \oplus B) + Cin(\overline{A \oplus B})$

$= \bar{C}in X + C\bar{in} \bar{X}$

$= Cin \oplus X$

$= Cin \oplus A \oplus B$

Carry

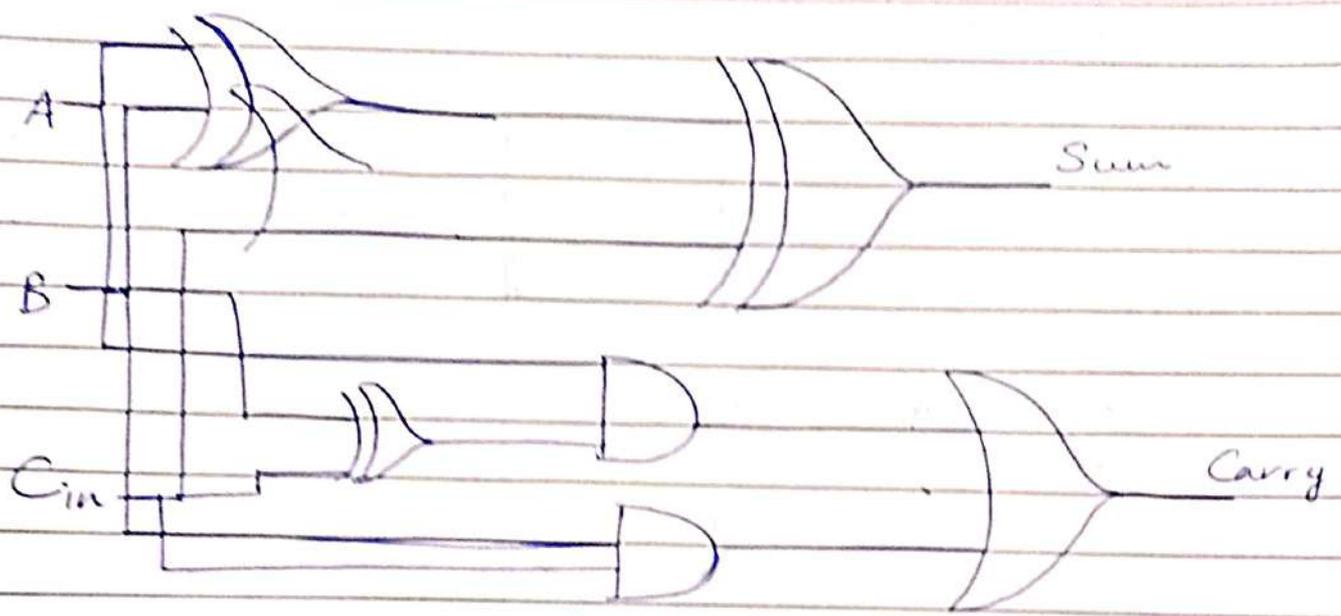
Cont K-Map:-

A \ BC _{in}	00	01	11	10
0	000	001	011	010
1	100	101	111	110

The K-map contains 1s in cells 1, 2, 3, 4, 5, 6, and 7.
 Groupings are shown: a vertical group of 1s in the 01 column (cells 1, 5), a horizontal group of 1s in the 11 row (cells 3, 7), and a large group of 1s in the 10 column (cells 2, 6).

$$\begin{aligned}
 & A\bar{B}C_{in} + BC_{in} + AB\bar{C}_{in} \\
 & = AC_{in}(\bar{B} + B) + B\bar{C}_{in} = A(\bar{B}C_{in} + BC_{in}) + B\bar{C}_{in} \\
 & = (A+B)C_{in} = A(B \oplus C_{in}) + B\bar{C}_{in}
 \end{aligned}$$

$$F(A, B, C) = B \cdot C_{in} + A \cdot C_{in} + A \cdot \bar{B}$$

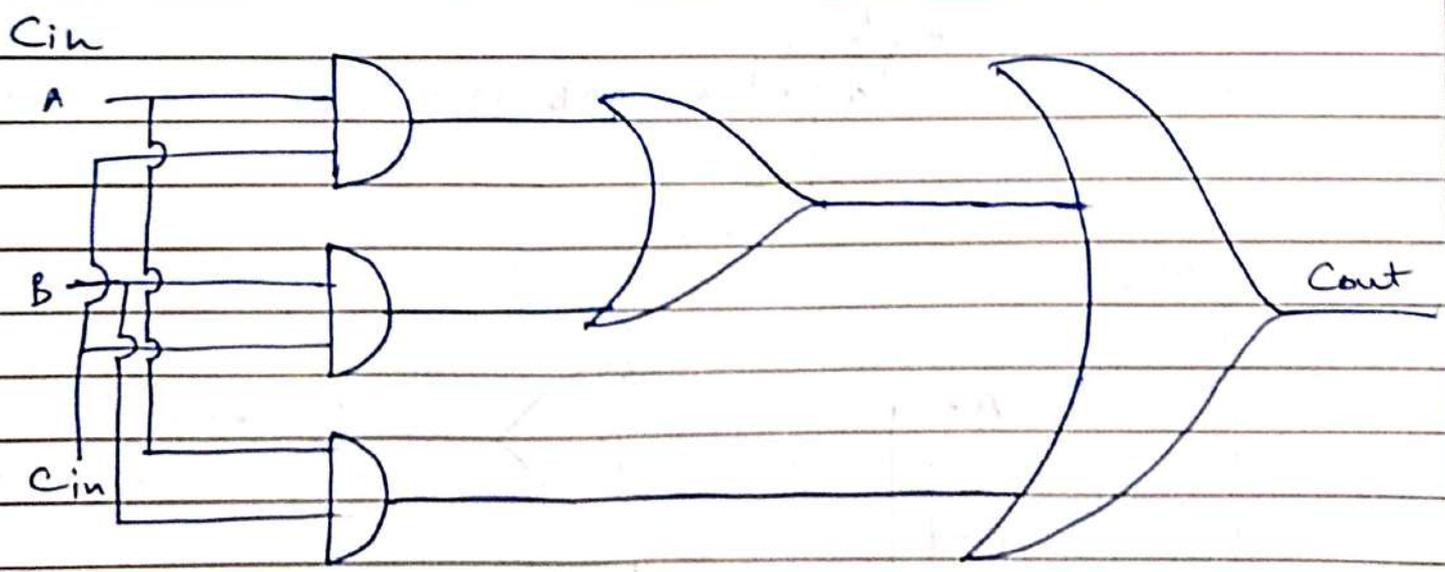


REMEMBER !!!

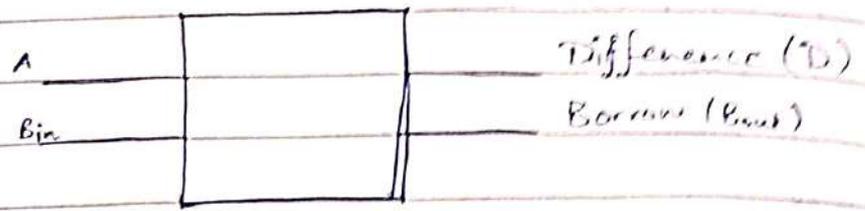
SOP	POS
A - 1	A - 0
A - 0	\bar{A} - 1

- You can't group odd number of outputs in K-maps
- if you grouped $(B + \bar{B})$, don't group anything else.

SharkCoders



Half Subtractor



A	Bin	D	Bout
0	0	0	0
0	1	1	1
1	0	1	0
1	1	0	0

$$D = \bar{A}B$$

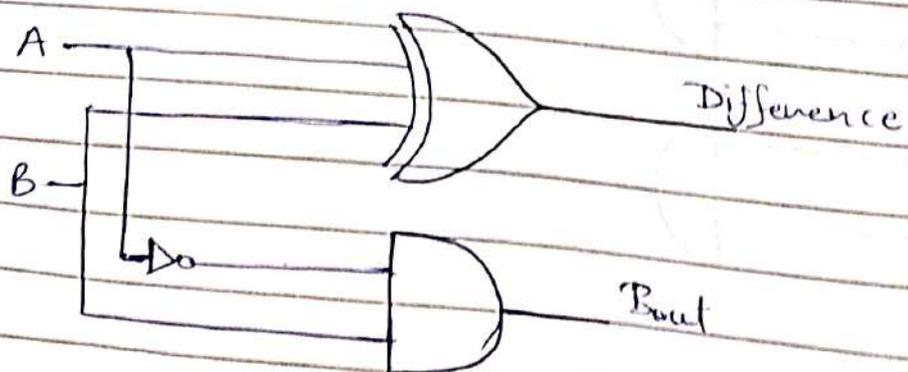
K-Map for D:-

	Bin		
A	0	1	
0	0	1	→ $\bar{A}B + A\bar{B} = A \oplus B$
1	1	0	

K-Map for Bout:-

	Bout		
A	0	1	
0	0	1	→ $\bar{A}B$
1	0	0	

Diagram:



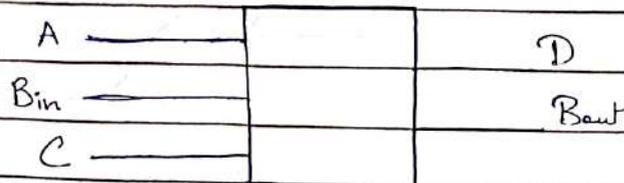
22/8/24

classmate

Date _____

Page _____

Full Subtractor



A	B _{in}	C	D	B _{out}
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	0	1
1	0	0	1	0
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1

K-Map for D :-

		B _{in} C				
	A	00	01	11	10	
	0	0	1	0	1	→ $A\bar{B}_in\bar{C} + \bar{A}\bar{B}_inC + AB_inC + \bar{A}B_in\bar{C}$
	1	1	0	1	0	

$$\begin{aligned}
 A\bar{B}_in\bar{C} + \bar{A}\bar{B}_inC + AB_inC + \bar{A}B_in\bar{C} &= A(\bar{B}_in\bar{C} + B_inC) + \bar{A}(\bar{B}_inC + B_in\bar{C}) \\
 &= A(\bar{B}_in \oplus C) + \bar{A}(B_in \oplus C) \\
 &= A(\bar{X}) + \bar{A}(X) \\
 &= A \oplus X \\
 &= A \oplus B_in \oplus C
 \end{aligned}$$

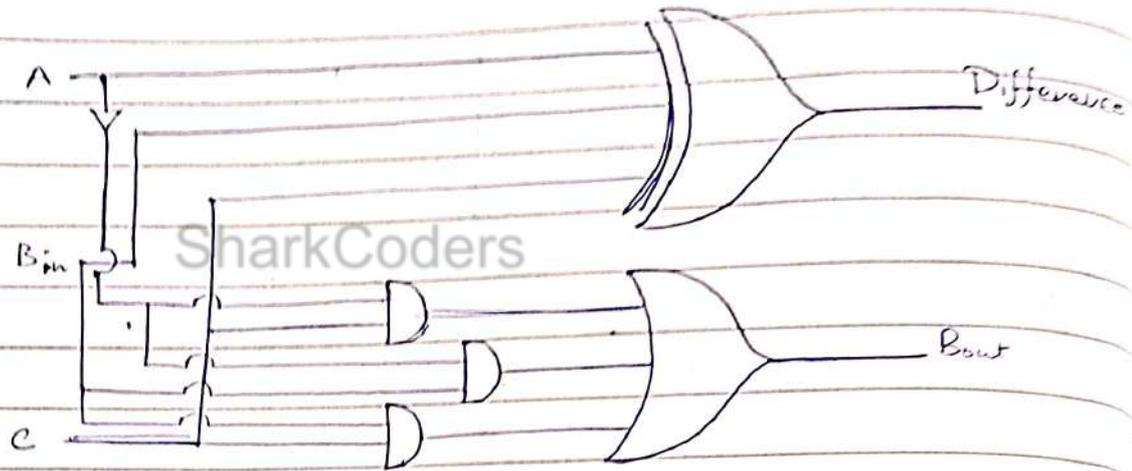
K-Map for B_{out} :-

		B _{in} C				
	A	00	01	11	10	
	0	0	1	1	1	→ $\bar{A}C + \bar{A}B_in + B_inC$
	1	0	0	1	0	

22/8/24

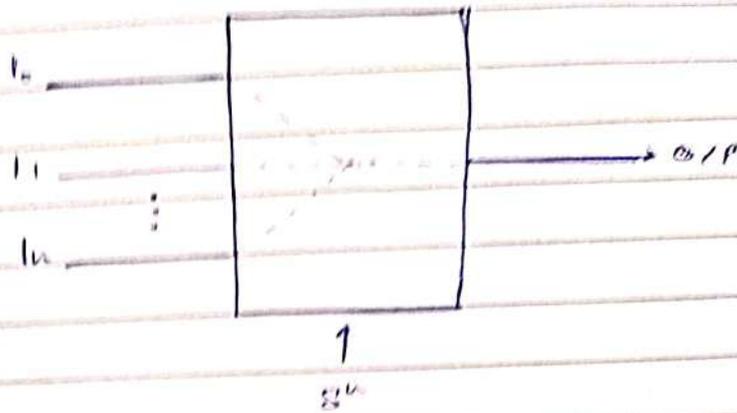
classmate
Date _____
Page _____

Diagram :-



Multiplexing

Multiplexing



- data selector
- many inputs and one output

MUX

2:1

4:1

→ 4 I/P lines

→ 4 I/P lines

→ 1 select line

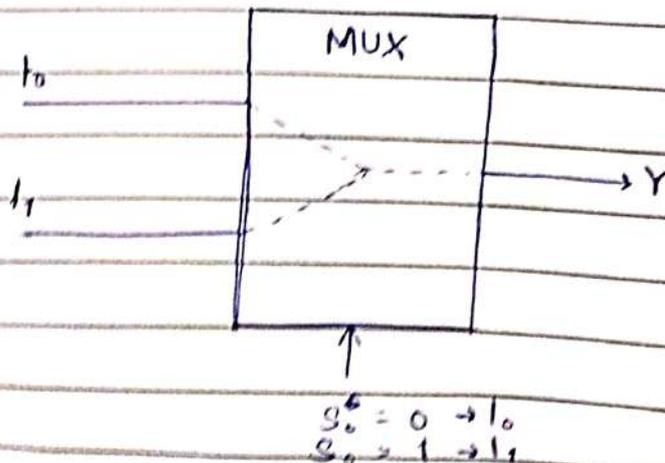
→ 2 select lines

→ 1 O/P line

→ 1 O/P line

2:1 MUX:

*



$S_0 = 0 \rightarrow I_0$
 $S_0 = 1 \rightarrow I_1$

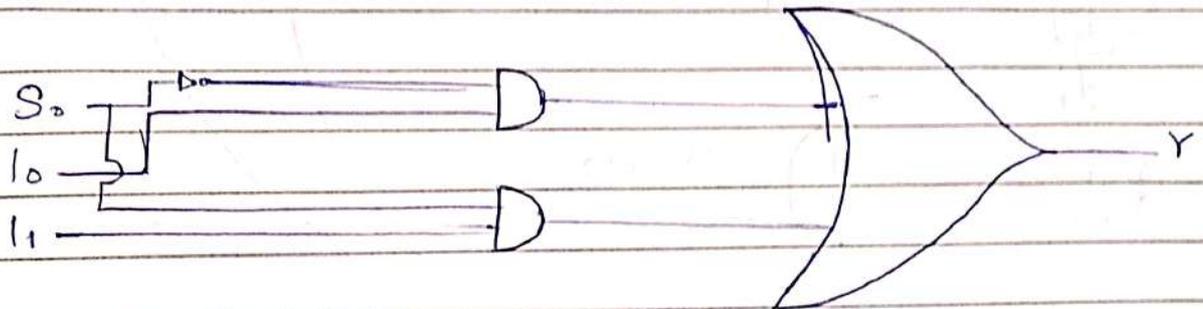
2/5/24

classmate

Date _____
Page _____

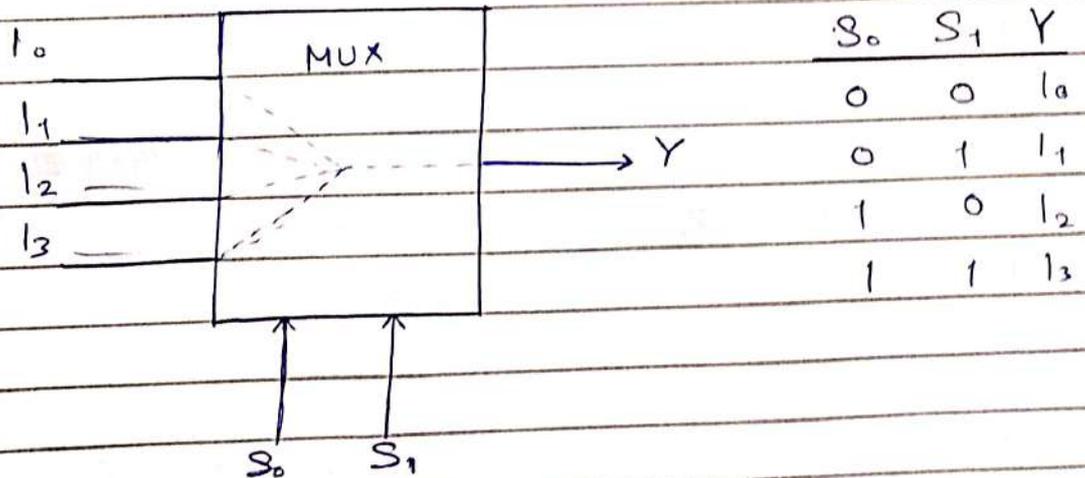
I_0	I_1	S_0	I_0	I_1	Y
0	0	0	0	x	0
0	1	0	1	x	1
1	0	1	x	0	0
1	1	1	x	1	1

$$Y = \bar{S}_0 I_0 + S_0 I_1$$



SharkCoders

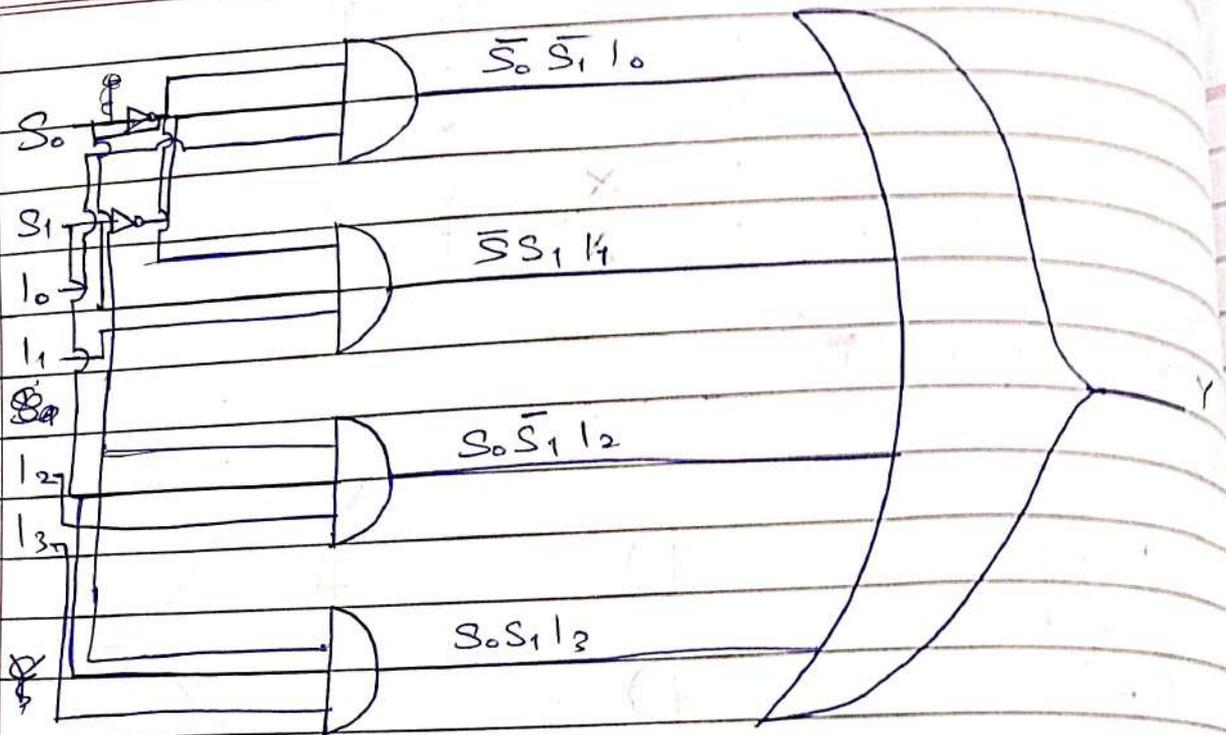
4:1 MUX



$$Y = \bar{S}_0 \bar{S}_1 I_0 + \bar{S}_0 S_1 I_1 + S_0 \bar{S}_1 I_2 + S_0 S_1 I_3$$

(NEXT PAGE)

2/9/24



Demultiplexer

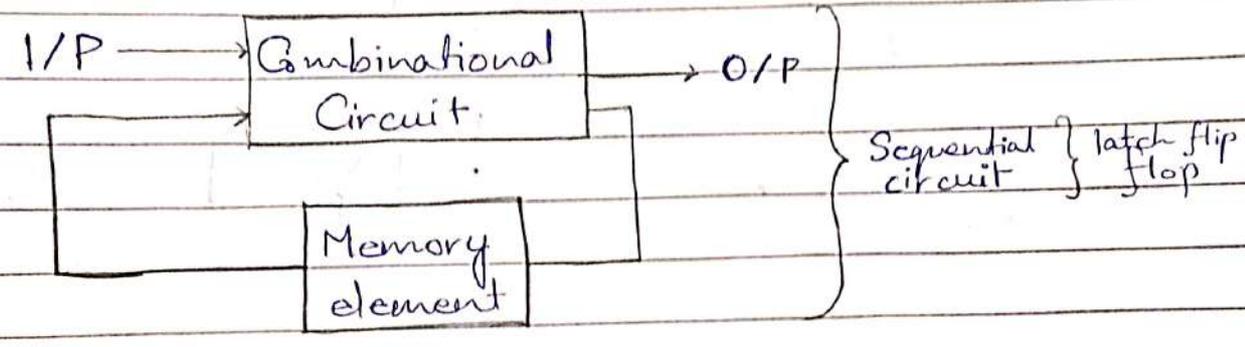
- truth tables are opposite outputs.

SharkCoders

- encoder
- BCD encoder
- Registers and types
- Universal shift register

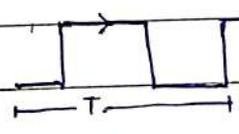
Flip Flops

Flip Flops



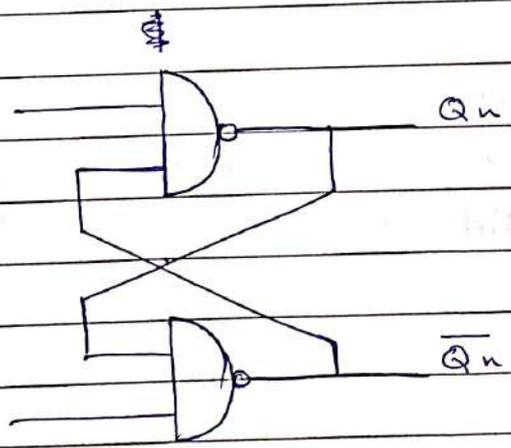
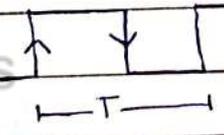
Latch

- no CLK (clock) pulse
- level triggered



Flip-Flops

- CLK (clock) pulse
- edge triggered

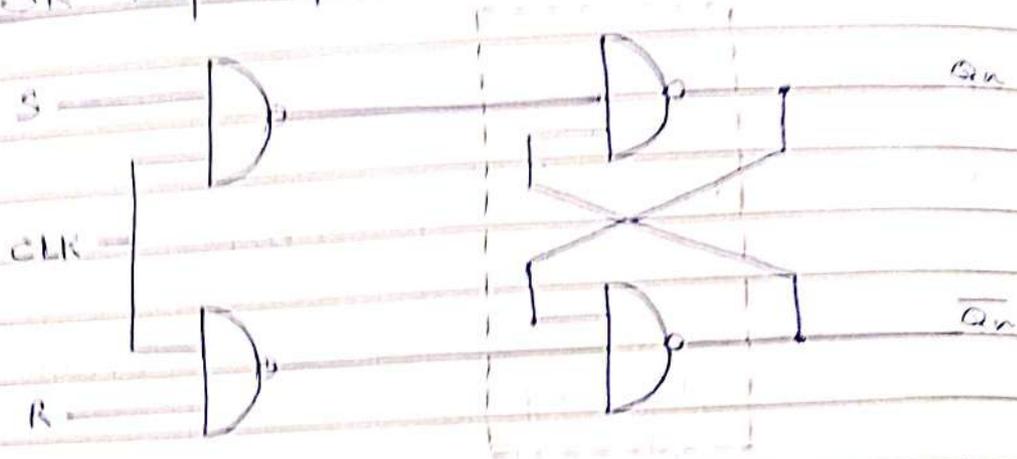


S	R	Q _n
0	0	Invalid
0	1	1
1	0	0
1	1	Hold

13/9/24

DATE
PAGE

SR Flip Flops



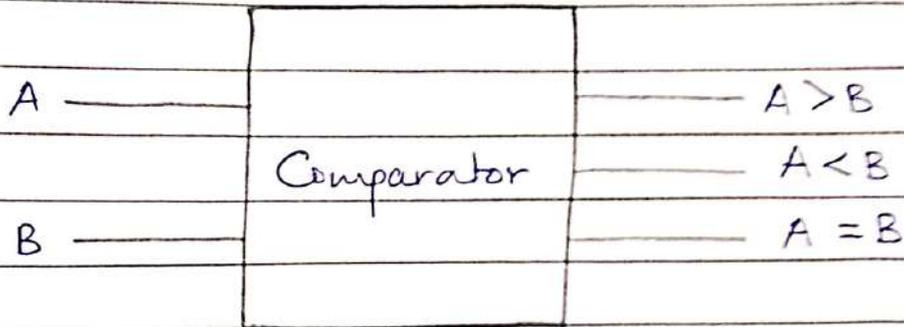
CLK	S	R	Latch
0	0	0	Invalid
0	1	0	1
1	0	0	0
1	1	0	Hold

CLK	S	R	Q_{n+1}
0	X	X	Q_n
1	0	0	Hold
1	0	1	0 (Reset)
1	1	0	1 (Set)
1	1	1	Invalid

BCD to 7 Segments conversion

Comparator:

1) Magnitude Comparator

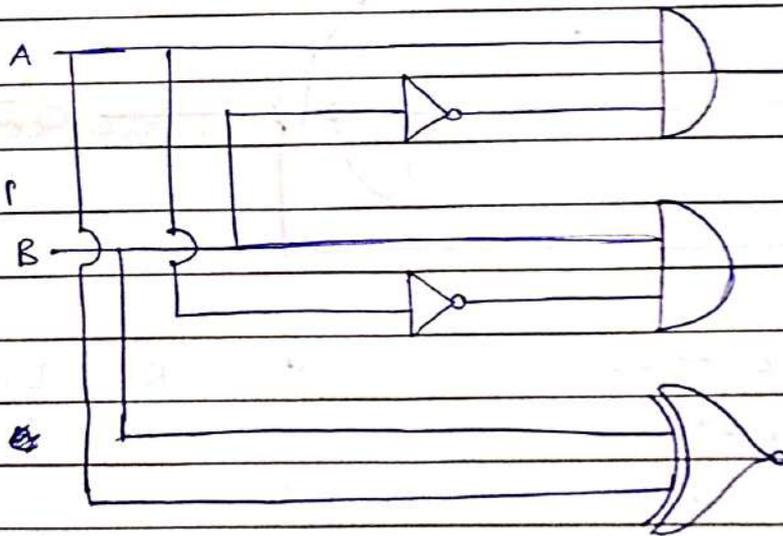


A	B	A > B	A < B	A = B
0	0	0	0	1
0	1	0	1	0
1	0	1	0	0
1	1	0	0	1

$$A > B \rightarrow A\bar{B}$$

$$A < B \rightarrow \bar{A}B$$

$$A = B \rightarrow \bar{A}\bar{B} + AB = A \text{ XNOR } B$$



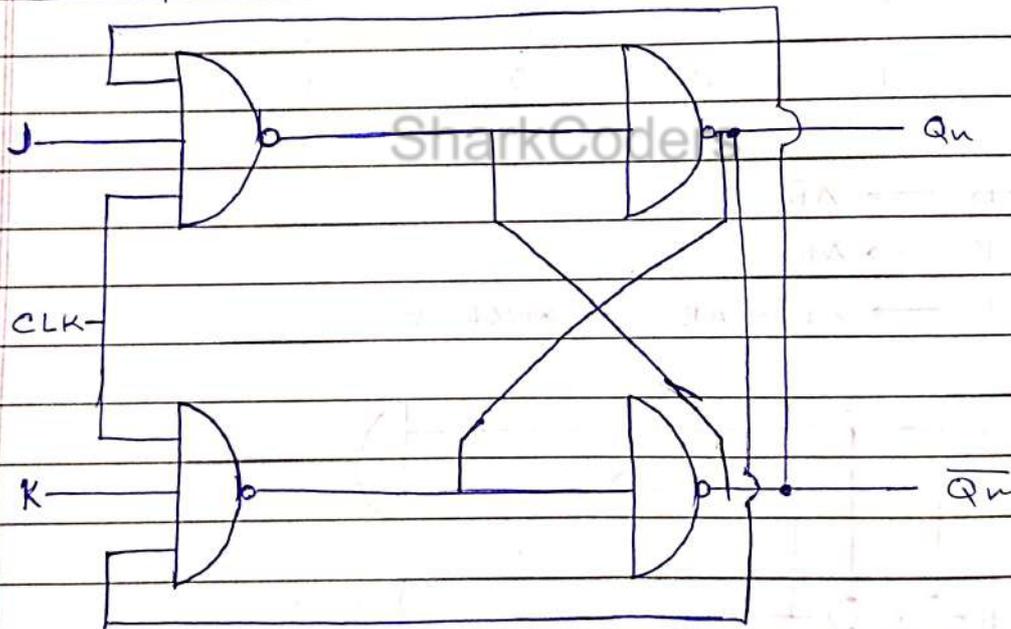
Lower Order Comparator to Higher Order

Cascading Comparator

A_0	A_0	
A_1	A_1	
A_2	A_2	$A > B$
A_3	A_3	$A < B$
b_0	b_0	$A = B$
b_1	b_1	
b_2	b_2	
b_3	b_3	
$A > B$		$A > B$
$A < B$		$A < B$
$A = B$		$A = B$

21/9/24

20/9/24 JK Flip Flops



Case I: $Q_n = 0$, then

$$Q_{n+1} = 1$$

\therefore It is toggling.

S	R	Latch
0	0	Invalid
0	1	1
1	0	0

Case II: $Q_n = 1$, then

$$Q_{n+1} = 0$$

\therefore It is toggling.

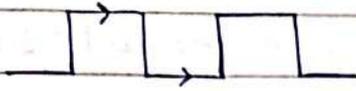
1	1	Hold
---	---	------

20/9/24

Race Around Condition

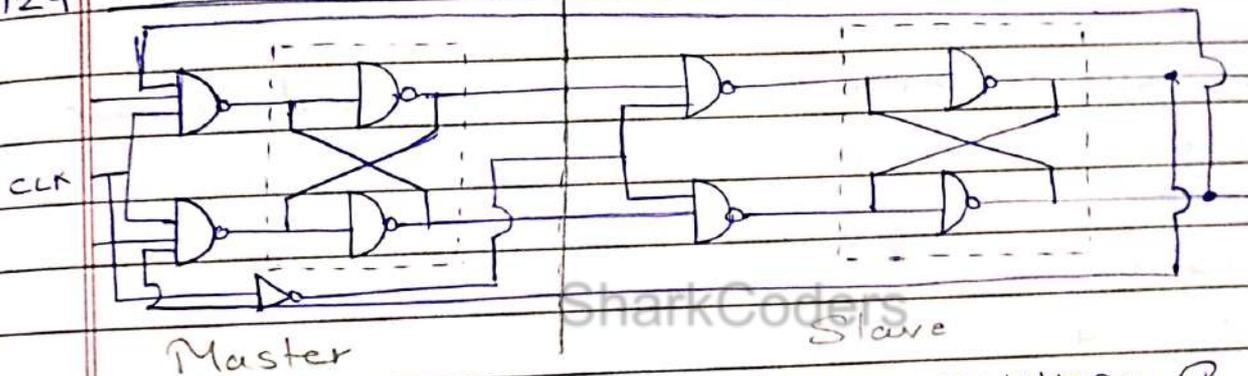
1. Level triggered JK F.F.

2. When $J = K = 1$



3. $T_w \gg T_d$ [$T_d = \text{propagation delay}$]
 $10\text{ns} \gg 2\text{ns}$

1/9/24 Master-Slave Flip-Flop



• This solves the ~~propagation delay condition~~ Race Around condition and prevents the toggling in output.

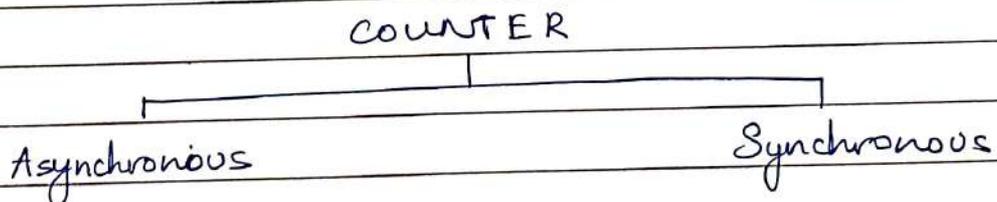
24/9/24

Counters

Device that stores the no. of times a particular event or process has occurred, ~~often~~ ^{often} in relationship to a clock signal.

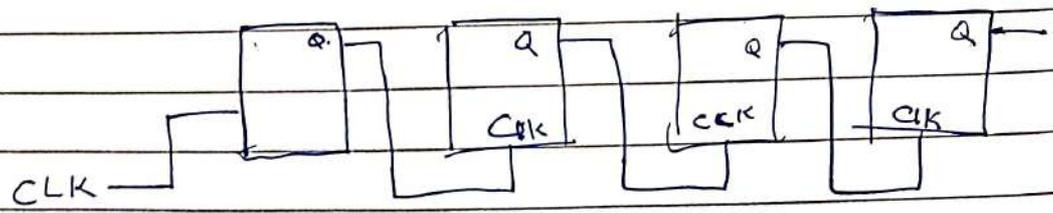
- counting purpose, count specific event happening in the circuit.
- E.g.: in UP counter, a counter ~~can~~ increase count for every rising edge of the clock.
- can follow certain sequence based on our design
- Properties
 - timing
 - sequencing
 - counting

SharkCoders



Asynchronous counter

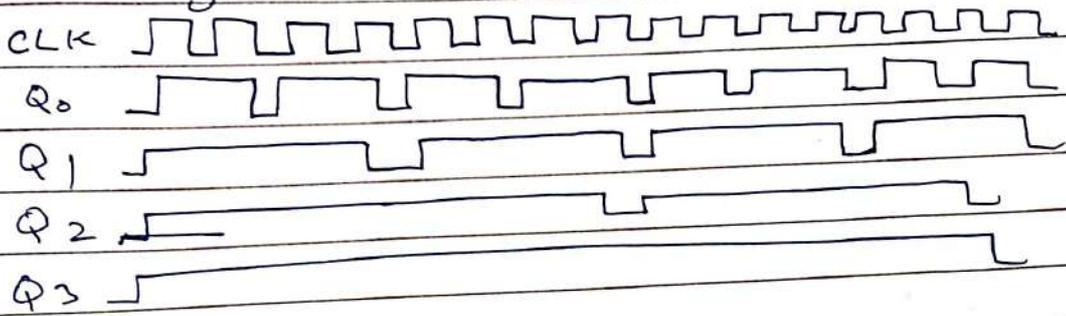
: no uni clock



24/9/24

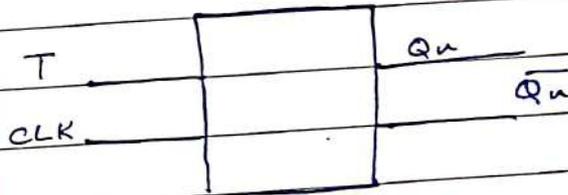
up counter - 1, 2, 3, ... n
down counter - n, n-1, n-2, ... 1

ripples are generated.



T-Flip Flop

T-toggle (switching between 0 and 1)



• When $T=0$, I/P is same as the O/P ($Q_{n+1} = Q_n$)
 $T=1$, O/P is $Q_n = \overline{Q_n}$

T	Q_n	Q_{n+1}
0	0	0
0	1	1
1	0	1
1	1	0

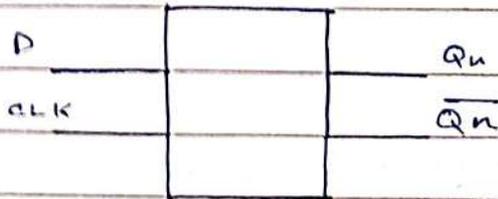
24/9/24

classmate

Date

Page

D flip Flop



- when $D = 0$, $O/P = 0$
 $D = 1$, $O/P = 1$

- $Q_{n+1} = D$

D	Q_n	Q_{n+1}
0	0	0
0	1	0
1	0	1
1	1	1

Synchronous Counter

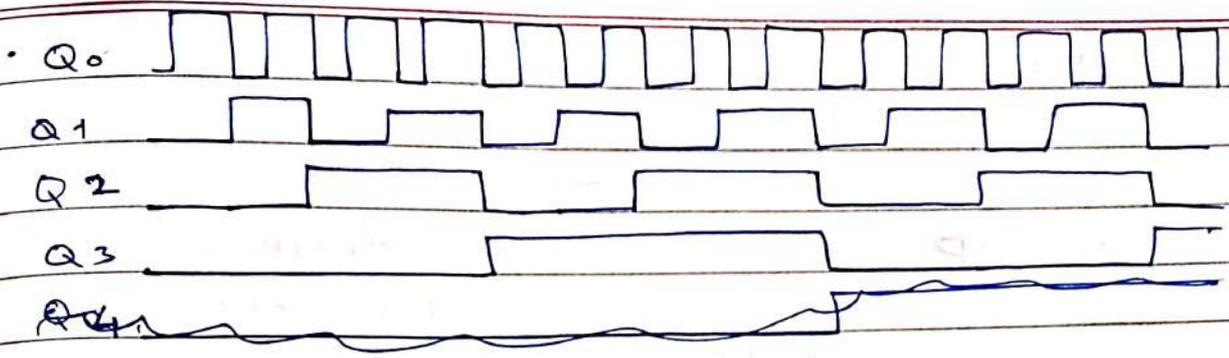
- one global clock which drives each flip flop so O/P changes in parallel.
- advantage: operate on a higher frequency than as it does not have cumulative delay because same clock is given to each flip flop.
- a.k.a. parallel counter.

24/9/24

classmate

Date _____

Page _____



Decade Counter

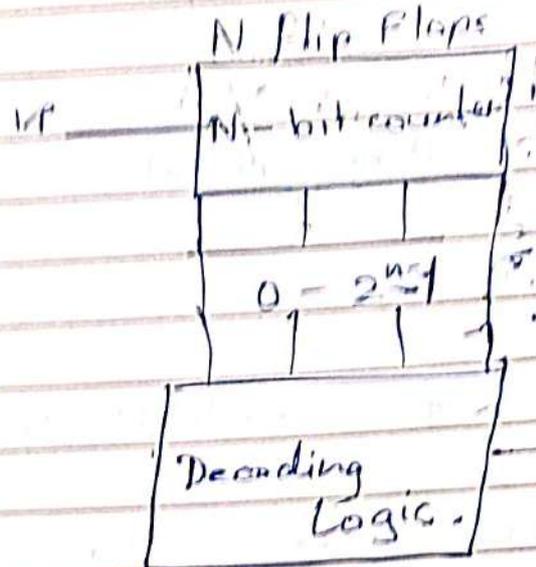
- counts 10 states then resets to its initial states.
- counts from 0 to 9
- can also go through 0 to 15. (for 4 bit counter)

CLK Pulse	Q3	Q2	Q1	Q0
0	0	0	0	0
1	0	0	0	1
2	0	0	1	0
3	0	0	1	1
4	0	1	0	0
5	0	1	0	1
6	0	1	1	0
7	0	1	1	1
8	1	0	0	0
9	1	0	0	1
10	0	0	0	0

CounterBinary Counter

up
0000 → 1111

down
1111 → 0000



→ ~~we~~ we can know when counter has reached a certain count

SharkCoders

Modulus

The no. of O/P states through which a counter before returning to its first state.

- BCD Counter

- 4-bit

- MOD - 10

Applications

- counting

- time measurement

- analog to digital converter

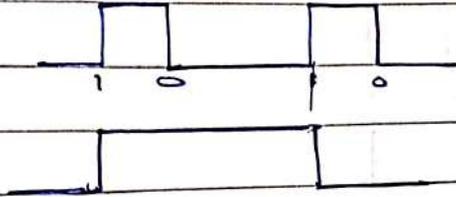
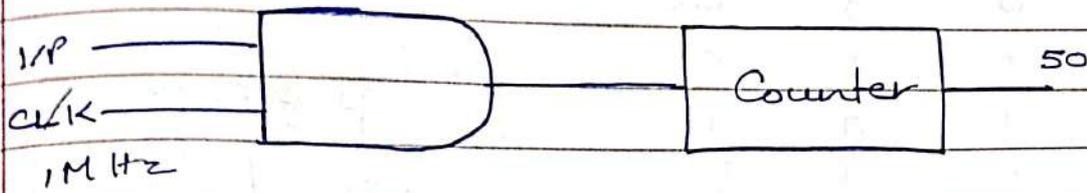
30/9/24

classmate

Date _____

Page _____

• frequency division



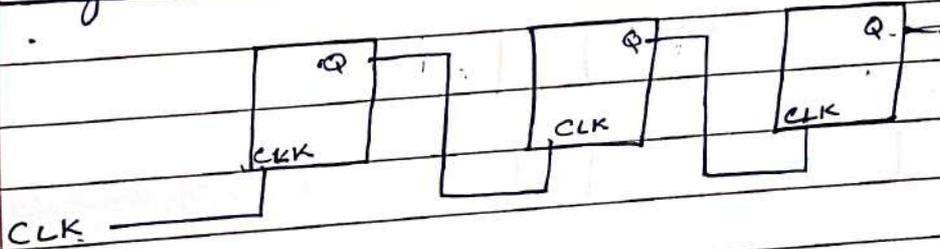
COUNTERS

async
(ripple)

sync.

SharkCoders

Asynchronous



• easy to design.

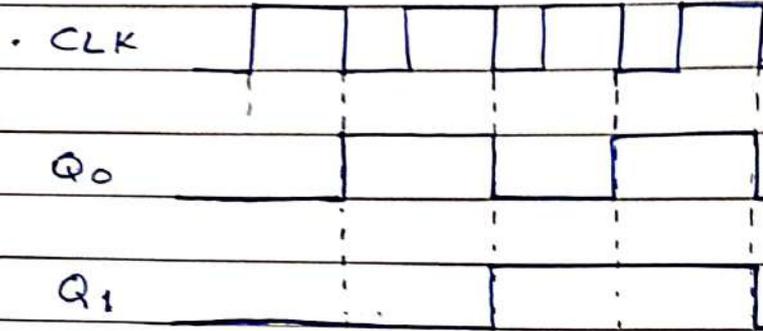
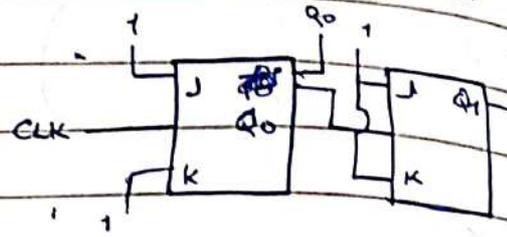
• cannot work for high speed operations.

~~Synchronous~~ toggle mode

30/9/24

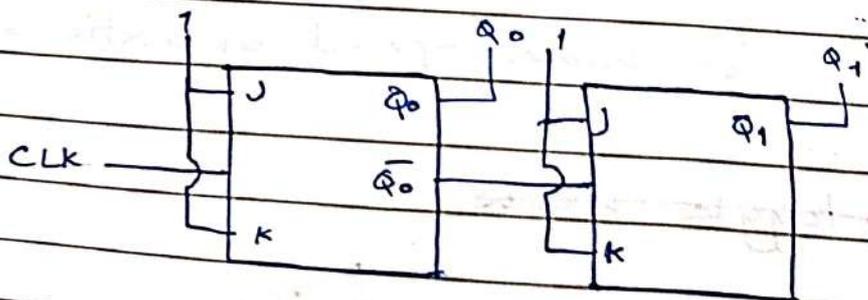
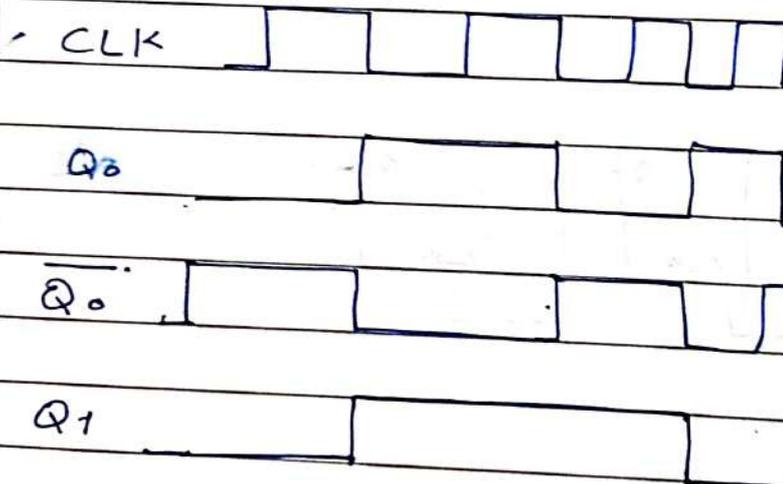
CLK	J	K	Q_{n+1}
↓	0	0	Q_n
↓	0	1	0
↓	1	0	1
↓	1	1	$\overline{Q_n}$

→ 2 bit bin. up.



• toggle state at every falling edge

2 bit bin. down

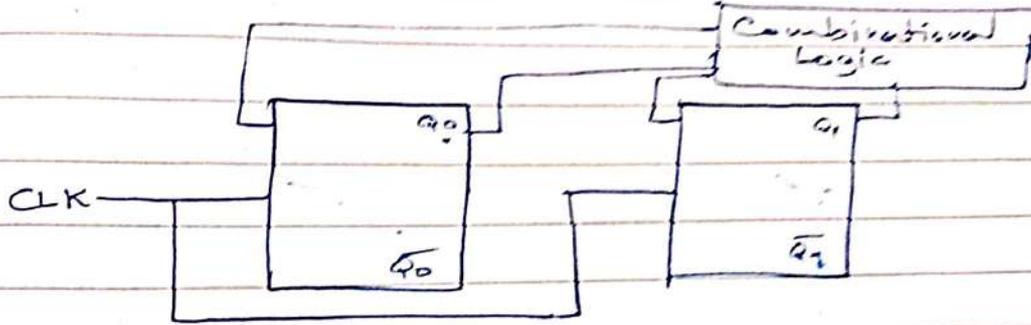


30/9/24

classmate
Date _____
Page _____

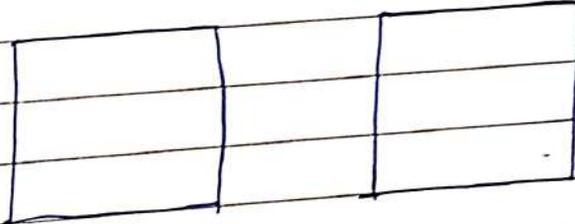
Synchronous

• all flip flops receive the CLK at the same time.



• Steps

- find the required no. of flip flops
- draw the state diagram
- select flip flop and draw excitation table
- min. expression of _____
- draw logic circuit



A	B
0	0
0	1
1	0
1	1

Q_n	Q_{n+1}	J	K
0	0	0	x
0	1	x	0
1	0	1	x
1	1	x	0

J	K	Q_n	Q_{n+1}
0	x	0	0
x	1	1	0
1	x	0	1
x	0	1	1

30/8/24

Present		Next		Propagation			
Q_0	Q_1	Q_0^+	Q_1^+	J_0	K_0	J_1	K_1
0	0	0	1	0	X	1	X
0	1	1	0	1	X	X	1
1	0	1	1	X	0	1	X
1	1	0	0	X	1	X	1

Max propagation Delay = $T_{PD} = T_{PD}(FF) + (n-2)T_{PD}(Mux)$

$$f_{clk(max)} = \frac{1}{T_{PD}}$$

SharkCoders

4/9/24

classmate

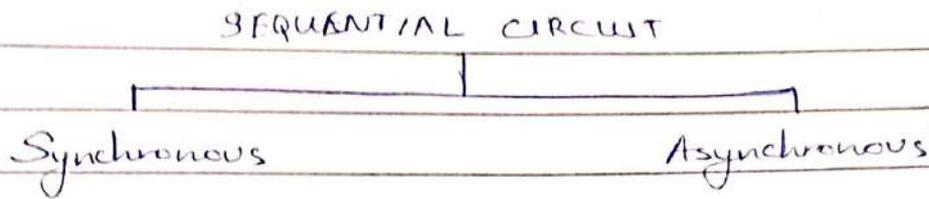
Date _____

Page _____

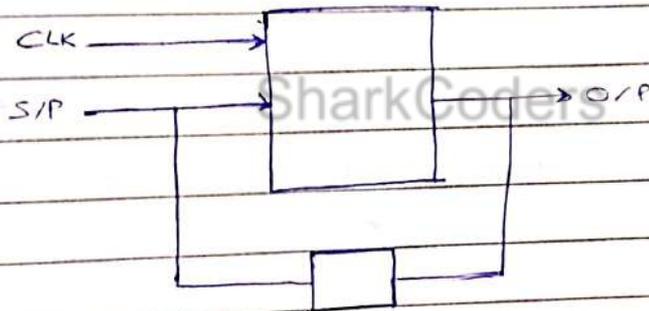
Sequential Circuits

Type of logic circuit whose O/P depends on the present value of its I/P signals but on the past history of its I/Ps.

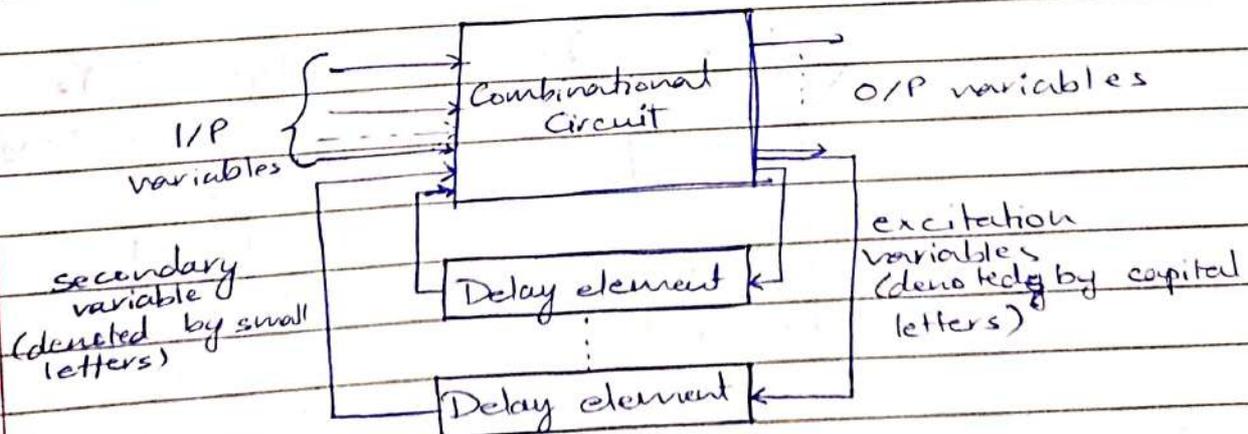
• has a state



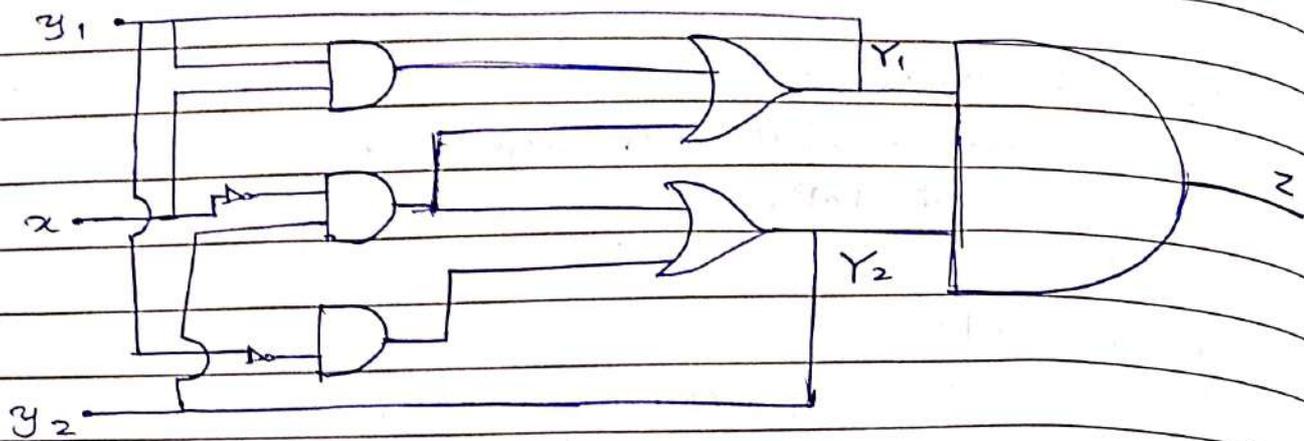
Synchronous S.A.



SA



4/9/24



Step I:

$$Y_1 = x y_1 + \bar{x} y_2$$

$$Y_2 = x \bar{y}_1 + x y_1$$

$$Z = Y_1 Y_2 = \bar{x} y_2$$

$$= Y_1 Y_2$$

$$= (x y_1 + \bar{x} y_2)(x \bar{y}_1 + x y_1)$$

$$= (x y_1)(x \bar{y}_1) + (x y_1)(x y_1) + (\bar{x} y_2)(x \bar{y}_1) + (\bar{x} y_2)(x y_1)$$

$$= \cancel{x y_1 x} \bar{y}_1 + x y_1 + \bar{x} y_2 x \bar{y}_1 + \bar{x} y_2 x y_1$$

$$= \bar{x} y_2 + x y_1$$

Step II:

$$y = x y_1 + \bar{x} y_2$$

Map of Y_1

$y_1 y_2 \backslash x$	0	1
00	0	0
01	1	0
11	1	1
10	0	1

Map of Y_2

$$y = x \bar{y}_1 + x y_2$$

$y_1 y_2 \backslash x$	0	1
00	0	1
01	1	1
11	1	0
10	0	0

4/9/24

classmate

Date _____
Page _____

Step II: Map of Z

$$Z = \bar{x}y_2$$

$y_1 y_2 \backslash x$	0	1
00	0	0
01	1	0
11	1	0
10	0	0

Step III: Transition table = combination of all secondary variable

$y_1 y_2 \backslash x$	0	1		
$Y_1 + Y_2 = a \rightarrow 00$	00	01	a	b
$b \rightarrow 01$	11	01	c	b
$c \rightarrow 11$	11	10	c	d
$d \rightarrow 10$	00	10	a	d

Step IV:

$$Y_1 + Y_2 + \dots \Rightarrow a, b, c, d \Rightarrow [a, z_1], [b, z_2], [c, z_3], [d, z_4]$$

$a, 0$	$b, 0$
$c, 1$	$b, 0$
$c, 1$	$d, 0$
$a, 0$	$d, 0$

7/10/24

Unit IV

Q.1. ★ Analyze an asynchronous sequential circuit with two external excitation functions with two feedback loops given as:

$$y_1 = xy_1 + \bar{x}y_2$$

$$y_2 = x\bar{y}_1 + \bar{x}y_2$$

a) Draw the logic diagram of the circuit

b) Derive the transition table and obtain the flow table

~~Ans. a)~~

Q.2. An asynchronous sequential circuit is described by the following excitation and O/P functions,

$$Y = x_1x_2 + y(x_1 + x_2).$$

$$Z = Y$$

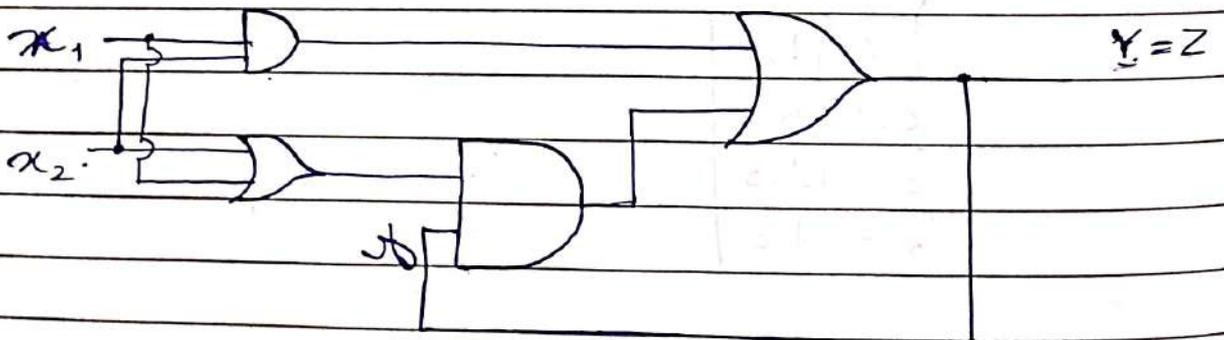
SharkCoders

a) Draw the logic diagram of the circuit

b) Derive the transition table, flow table and O/P map.

c) Describe the behaviour of the circuit.

Ans. a) The logic diagram



7/10/24

classmate

Date _____

Page _____

b) The truth table

y	x_1	x_2	$x_1 x_2$	$y(x_1 + x_2)$	Y	Z
0	0	0	0	0	0	0
0	0	1	0	0	0	0
0	1	0	0	0	0	0
0	1	1	1	0	1	1
1	0	0	0	0	0	0
1	0	1	0	1	1	1
1	1	0	0	1	1	1
1	1	1	1	1	1	1

y	$x_1 x_2$			
	00	01	11	10
0	0	0	1	0
1	0	1	1	1

SharkCoders

SharkCoders

Join our whatsapp group